

Local Projections vs. VARs for Structural Parameter Estimation

Juan Castellanos

Bank of England

20th Annual Dynare Conference

June 2nd, 2026

Disclaimer: The views expressed in this presentation are my own and do not necessarily reflect those of the Bank of England nor its committees.



Motivation

- Starting with Jordà (2005), **local projections** (LP) have become a common tool to understanding the dynamic effects of economic shocks
 - * An alternative to vector autorregresions (VARs) when estimating impulse responses
- Other studies analyze the performance of these two models when estimating IRFs
 - * VARs and LPs estimate the same impulse responses in population (Plagborg-Møller and Wolf, 2020)
 - * However, there is a bias-variance trade off in finite samples (Li et al., 2024)
- My focus is instead on the **structural parameters** of any DSGE model
 - * Follow Smith (1993) in estimating structural parameters through an indirect inference exercise in which the auxiliary model is a macro-econometric model
- *How should we **choose between VARs and LPs** when estimating – via **minimum distance** – the structural parameters of our DSGE model?*

MONTE-CARLO EXPERIMENTS

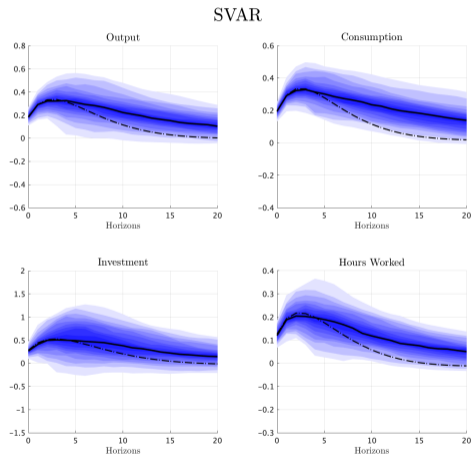
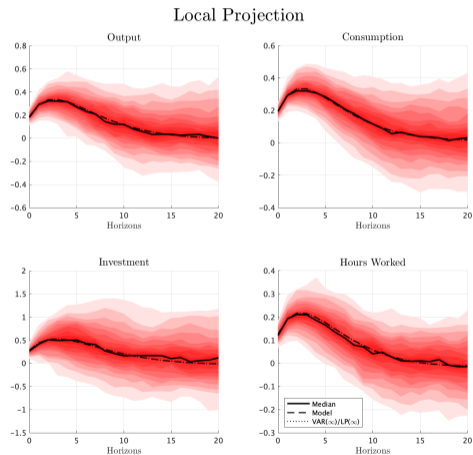
The DGP & the hyper-parameters

- The **log-linearized version of the Smets and Wouters (2007)** model is used to generate **S repeated samples** of macroeconomic aggregates
- The model is simulated each time at the estimated values from their paper using a sample of **T observations**
 - * $T = 300$ used as baseline
 - * $T = 100$ to address the issue of small sample bias of LPs (Herbst & Johannsen, 2023)
- We concentrate in **8 structural parameters** of the model:
 - * σ_c : intertemporal elasticity of substitution
 - * h : habit parameter
 - * σ_l : elasticity of labor supply
 - * φ : investment adjustment cost parameter
 - * ξ_w, ξ_p : Calvo adjustment probabilities
 - * ι_w, ι_p : Degree of indexation to past inflation
- **Simulated series are 10 times larger** than the sample size during the optimization stage
- The importance of the coefficients used to summarize the data is **weighted** by a squared matrix **W**
 - * Identity matrix: I_m
 - * Inverse of the VCM of the moments: Ω^{-1}
 - * Diagonal matrix with $1/h$ elements: I_d

Targeted Responses

- We focus on the **estimated impulse responses of four variables**: *output, consumption, investment and hours worked* to one of **three main aggregate shocks**: *monetary policy, fiscal policy and technology*
- Shocks are treated by the econometrician as
 - * *observed*, i.e. $\tilde{x}_t = \eta_t^i$
 - * *inferred via recursive ordering*
 - * *observed with error*, i.e. $\tilde{x}_t = \eta_t^i + \sigma_v v_t$
- The IRFs are estimated using a **VAR** or a **Local Projections**.
 - * If the sample size is small ($T = 100$), we also consider the bias-corrected LP (Herbst & Johansen, 2023) or the procedure by Killian (1998) for the SVAR
- In either case, the econometrician still needs to decide on at least two more things:
 - * The impulse response horizon, H . We set $H = 20$.
 - * The number of lags, p . We experiment with various p 's, i.e. $p \in \{2, 4, 8, 12\}$.

Targeted Impulse Responses (S=100, T=300, p=4)



Impulse Response Matching vs. Indirect Inference

- When estimating a subset of the structural parameters Θ of any DSGE model by matching impulse responses, there are two approaches:

- * **Target empirical** responses but **match with model** impulse responses

$$J^{irf} = \min_{\Theta} (\beta - \text{IRF}(\Theta))' W (\beta - \text{IRF}(\Theta)) \quad (1)$$

- It doesn't require a simulated dataset, only structural IRFs

- * **Target and match with** empirical responses

$$J^{smm} = \min_{\Theta} (\beta - \beta(\Theta))' W (\beta - \beta(\Theta)) \quad (2)$$

- It uses the same econometric approach in the real and simulated data

- How does the **choice of the econometric model** affects parameter estimates?

- * J^{irf} speaks about potential misspecification of the model economy
- * J^{smm} relates to misspecification of both the model and the binding function

How to assess the performance of the estimation?

- Overall performance

$$J^* = (\text{IRF}(\Theta^*) - \text{IRF}(\hat{\Theta}))' (\text{IRF}(\Theta^*) - \text{IRF}(\hat{\Theta})) \quad (3)$$

$$J^{smm} = (\beta(\Theta^*) - \beta(\hat{\Theta}))' (\beta(\Theta^*) - \beta(\hat{\Theta})) \quad (4)$$

$$J^{irf} = (\beta(\Theta^*) - \text{IRF}(\hat{\Theta}))' (\beta(\Theta^*) - \text{IRF}(\hat{\Theta})) \quad (5)$$

- Parameter-by-parameter performance

$$\mathcal{L}_\omega(\hat{\Theta}_i, \Theta_i^*) = \omega \times \underbrace{(\mathbb{E}[\hat{\Theta}_i] - \Theta_i^*)^2}_{\text{bias}} + (1 - \omega) \times \underbrace{\text{Var}(\hat{\Theta}_i)}_{\text{variance}} \quad (6)$$

- Model fit

- * Similar to (3), compute the unweighted distance between the structural IRFs but to other non-targeted shocks in the economy
- * For example, if targeting monetary policy shocks, look at fiscal and technology

5 MAIN LESSONS

1. IRF matching is more **sensitive to bias** in targeted responses and hence using LP-IRFs is preferable, while Ind. Inf. is **robust to misspecification** and hence benefits from the lower variance of VAR-IRFs.
2. When the lag length p is large, then IRFs and estimated parameters are **similar** independently of the econometric model. On the other hand, when p is small, LP-IRFs are less biased and hence better for IRF matching, while SVAR-IRFs have a larger bias but lower variance and hence better for Ind. Inf.
3. **Small sample bias** worsens the performance of the estimation specially for IRF matching when bias correction partly offsets the problem.
4. **Incorrect recursive identifications** are not an issue for parameter estimation when employing Ind. Inf.. Not true for IRF matching.
5. **Measurement error** worsens the structural estimation outcome and unit normalization only ameliorates the problem.

LESSONS 1, 2 & 3:
OBSERVED SHOCK ASSUMPTION

IRF matching vs. Indirect Inference

- Simplifying assumptions for comparison:
 - * Observed shock assumption
 - * Target IRFs estimated with a LP or SVAR model and $T = 300$ observations
 - * Weight all responses equally during the estimation stage, i.e. $W = I$
- **Overall performance measures** are averaged across estimations using different lag lengths ($p \in \{2, 4, 8, 12\}$) and shocks (TFP, fiscal, monetary)

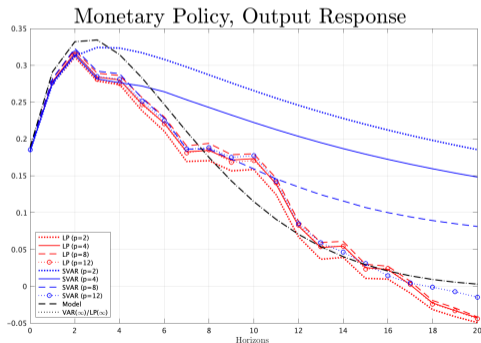
| | IRF matching | | | | Indirect Inference | | | |
|-------------------------|--------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| <i>Local Projection</i> | 35.10 | 0.27 | 3.49 min | 18.70 | 32.54 | 0.39 | 42.88 min | 17.91 |
| <i>Structural VAR</i> | 35.23 | 0.41 | 3.93 min | 17.93 | 33.87 | 0.33 | 14.47 min | 18.39 |

Lag length and IRF matching

- In the IRF matching estimator we are minimizing a distance that can be decomposed as:

$$\underbrace{[\beta(p, T|\Theta) - \beta(p, T = \infty|\Theta)]}_{\text{small sample bias}} + \underbrace{[\beta(p, T = \infty|\Theta) - IRF(\Theta)]}_{\text{lag truncation bias}} \quad (7)$$

- *Small sample bias* is common to both Local Projections and VARs
- *Lag truncation bias* only matter for VARs!
 - * Local Projection IRFs are independent of the lag length when the shock is observed
 - * VAR IRFs are heavily biased at short lag lengths and this truncation bias shrinks as we increase p



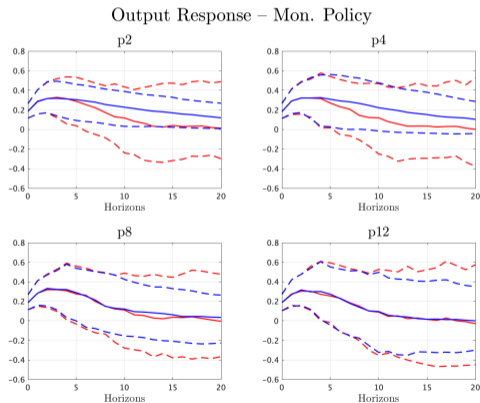
Lag Length and Indirect Inference

- Point estimates

- * Local Projection IRFs are independent of the lag length when the shock is observed
- * SVAR IRFs approximately agree with LP IRFs up to horizon p , then extrapolates using the first p sample autocovariances

- Confidence Intervals

- * Local Projection IRFs have a much wider bands, specially at long horizons
- * SVAR IRFs converge towards the sample uncertainty of LPs as p gets large

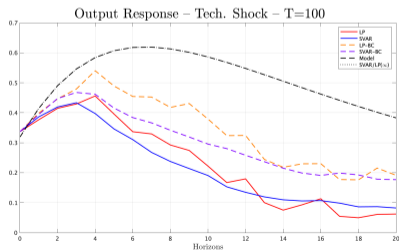
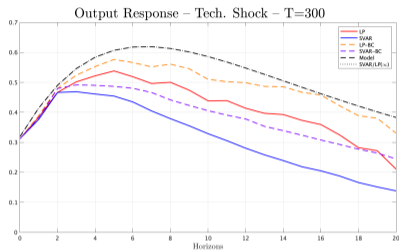


Decomposition by lag length

| | IRF matching | | | | Indirect Inference | | | |
|-------------------------|--------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| | p=2 | | | | | | | |
| <i>Local Projection</i> | 35.75 | 0.24 | 3.30 min | 18.97 | 25.47 | 0.34 | 18.93 min | 18.02 |
| <i>Structural VAR</i> | 34.61 | 0.61 | 4.32 min | 17.00 | 26.25 | 0.16 | 11.88 min | 19.32 |
| | p=4 | | | | | | | |
| <i>Local Projection</i> | 35.68 | 0.25 | 3.40 min | 18.74 | 30.26 | 0.37 | 28.99 min | 17.95 |
| <i>Structural VAR</i> | 36.01 | 0.39 | 3.89 min | 17.75 | 31.49 | 0.26 | 15.35 min | 18.26 |
| | p=8 | | | | | | | |
| <i>Local Projection</i> | 34.69 | 0.28 | 3.83 min | 18.47 | 35.91 | 0.44 | 45.06 min | 17.69 |
| <i>Structural VAR</i> | 34.92 | 0.34 | 3.85 min | 18.36 | 37.26 | 0.49 | 13.35 min | 18.01 |
| | p=12 | | | | | | | |
| <i>Local Projection</i> | 34.27 | 0.29 | 3.44 min | 18.63 | 38.52 | 0.41 | 78.53 min | 17.98 |
| <i>Structural VAR</i> | 35.39 | 0.30 | 3.67 min | 18.61 | 40.47 | 0.41 | 17.29 min | 17.98 |

Small sample bias & bias correction

- P-M & W (2023) show that $LP(p)$ exactly agree with true responses and that $SVAR(p)$ agrees up to lag p
- However, **sample uncertainty** matters!
 - * In finite samples, e.g. $T = 300$, both LP and SVAR are biased after horizon p , with SVARs having a more severe bias as long as the response is persistent
 - * The sample size typically found in empirical applications is even shorter and around $T=100$ (H&J, 2023), which makes these biases worse.
- **Bias correction** partially offsets the small sample bias, but two questions arise in our context
 - * Q1: Does Indirect Inference improves upon IRF matching when this bias is severe?
 - * Q2: Does targeting bias corrected responses improve the model estimation?



IRF matching vs. Indirect Inference in small samples

- Higher sample uncertainty associated with fewer observations ($T = 100$) leads to a **worse fit** of the model **for both estimation strategies**
- IRF matching suffers more its consequences as **Ind. Inf. is robust to misspecification** of the binding function
- For the same reason, applying **bias correction** to the targeted IRFs is more useful for IRF matching

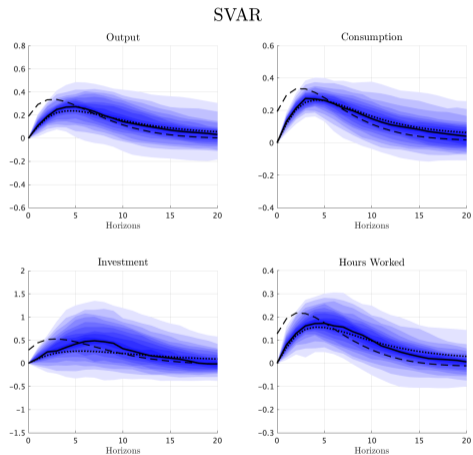
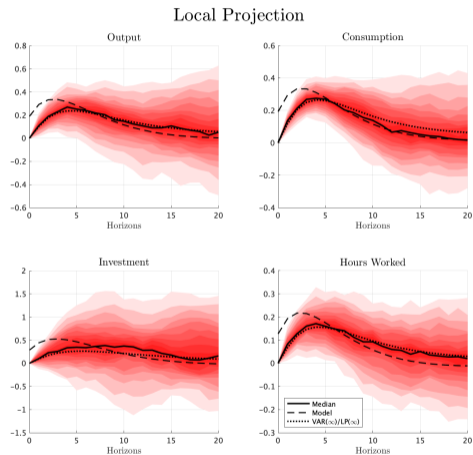
| | IRF matching | | | | Indirect Inference | | | |
|----------------------------|--------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| T=300 | | | | | | | | |
| <i>Local Projection</i> | 35.10 | 0.27 | 3.49 min | 18.70 | 32.54 | 0.39 | 42.88 min | 17.91 |
| <i>Structural VAR</i> | 35.23 | 0.41 | 3.93 min | 17.93 | 33.87 | 0.33 | 14.47 min | 18.39 |
| T=100 | | | | | | | | |
| <i>Local Projection</i> | 29.71 | 0.53 | 3.56 min | 18.13 | 22.00 | 0.46 | 18.46 min | 19.03 |
| <i>Structural VAR</i> | 31.62 | 0.47 | 3.33 min | 17.98 | 25.16 | 0.36 | 9.78 min | 19.50 |
| <i>Bias Corrected LP</i> | 31.55 | 0.32 | 3.26 min | 19.18 | 23.29 | 0.35 | 20.48 min | 19.50 |
| <i>Bias Corrected SVAR</i> | 33.48 | 0.32 | 3.42 min | 18.65 | 26.06 | 0.33 | 11.02 min | 20.11 |

LESSON 4:
RECURSIVE IDENTIFICATION

Cholesky Orthogonalized Shocks

- Shocks are not observable in applied work. Thus, there is a need for **identification**
- The most commonly used identification method in macroeconomics imposes **recursive zero restrictions on contemporaneous coefficients**
- As shown by Ramey (2016), there are two widely used alternatives:
 - * *Policy variable does not respond within the period to the other endogenous variable*
 - We use this assumption to identify **technology shocks** and **government spending shocks** within the Smets and Wouters model
 - TFP and government spending are the policy variables, ordered first. Output, consumption, investment and hours worked are included in the VAR or as lagged controls in the LP
 - * *Other endogenous variables do not respond to the policy shock within the period*
 - We use this assumption to identify **monetary policy shocks** within the Smets and Wouters model
 - We order the policy rate last in a VAR that also includes output, consumption, investment, hours worked, wages, and inflation. Similarly, these variables are added as contemporaneous controls in the LP

Mon. policy: real variables respond at $t = 0$ in the Sm & Wo model



Monetary policy: overall performance

- Main results still hold when targeting IRFs to monetary policy shock and it is a **better idea** in the Smets-Wouters world: lower J_{unt}^*
- When *identification assumption are incorrect*, then **Ind. Inf. is robust to such misspecification**
 - * Targeting consistently wrong responses helps with parameter identification as long as they have low variance

| | IRF matching | | | | Indirect Inference | | | |
|------------------|------------------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| | <i>Observed Shock</i> | | | | | | | |
| Local Projection | 50.65 | 0.07 | 3.46 min | 9.36 | 48.46 | 0.31 | 41.39 min | 9.40 |
| Structural VAR | 54.07 | 0.11 | 4.38 min | 9.26 | 53.60 | 0.30 | 14.65 min | 9.44 |
| | <i>Recursive Shock</i> | | | | | | | |
| Local Projection | 48.11 | 0.29 | 3.34 min | 9.60 | 56.91 | 0.18 | 78.57 min | 9.34 |
| Structural VAR | 47.09 | 0.34 | 3.78 min | 9.31 | 58.70 | 0.12 | 11.44 min | 9.34 |

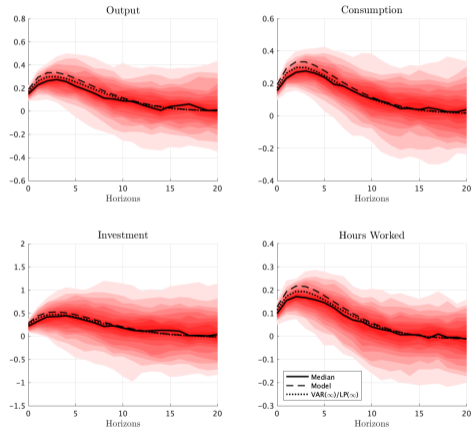
LESSON 5: MEASUREMENT ERROR

Direct measures of the shock of interest

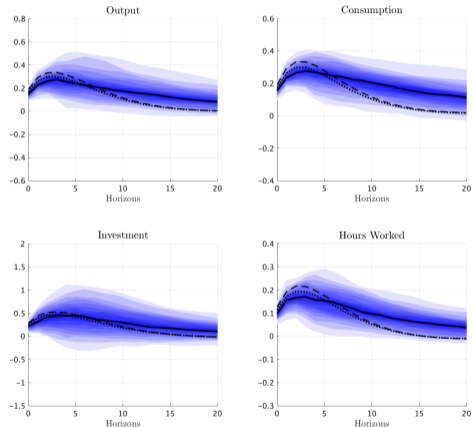
- A popular identification approach consist of constructing a series from historical documents to identify policy shocks, e.g.
 - * Romer and Romer (2004) monetary shock series based on FOCM meetings
 - * Ramey (2011) defense news series based on *Business Week* articles
- These series are used in dynamic single equation regressions or embedded in a Choleski decomposition, as we have done for the observed shock scheme
- In practice, there are good reasons to expect that these shocks suffer from **measurement error** or capture only part of the shock. Hence, I distinguish 3 cases:
 1. Study classical measurement error case, $\eta_t^{obs} = \eta_t + \sigma_v v_t$
 2. Proxy is correlated with other shocks, e.g. government spending with technology shock
 3. Unit normalization (Stock & Watson, 2018)

Attenuation bias in IRFs

Local Projection



SVAR



Stock & Watson unit normalization

- Unit normalization corrects the bias in estimated responses through rescaling.
- Great fix for the structural estimation as well, specially for *IRF matching*.

| | IRF matching | | | | Indirect Inference | | | |
|--|--------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| <i>True Monetary policy shock (η_t^m)</i> | | | | | | | | |
| <i>Local Projection</i> | 50.65 | 0.07 | 3.46 min | 9.36 | 48.46 | 0.31 | 41.39 min | 9.40 |
| <i>Structural VAR</i> | 54.07 | 0.11 | 4.38 min | 9.26 | 53.60 | 0.30 | 14.65 min | 9.44 |
| <i>Proxied monetary policy shock ($\eta_t^{a,obs} = \eta_t^a + \sigma_v v_t$)</i> | | | | | | | | |
| <i>Local Projection</i> | 1.79 | 1.25 | 3.05 min | 34.30 | 1.35 | 1.40 | 40.23 min | 33.31 |
| <i>Structural VAR</i> | 3.41 | 1.70 | 2.80 min | 33.47 | 1.70 | 1.18 | 13.74 min | 34.39 |
| <i>A 1% increase in r_0 (Stock and Watson (2018) normalization)</i> | | | | | | | | |
| <i>Local Projection</i> | 50.77 | 0.08 | 3.83 min | 19.34 | 49.49 | 0.52 | 49.84 min | 17.85 |
| <i>Structural VAR</i> | 53.41 | 0.32 | 4.04 min | 18.86 | 51.23 | 0.42 | 12.49 min | 17.93 |

KEY MESSAGE

*(Indirect Inference > IRF Matching)**

** LPs + IRF Matching can still be the most accurate option
conditional on correct identification and a sufficiently long sample*

APPENDIX

DATA GENERATING PROCESS

The Model Economy

- The discussion about which binding function to use, VAR or LP, is best made in the context of a specific model, but **which model to use?**
- **Many applications** that estimate their economies by matching impulse responses **concern linearized models**, e.g. Rotemberg and Woodford (1998), Christiano et al. (2005), Iacoviello (2005), etc.
 - * Indirect inference was initially proposed as a method to estimate non-linear models
 - * Nonetheless we still need to understand how to choose the binding function in this simpler set up
- The responses to monetary, fiscal and technology shocks are the most widely studied in empirical applications (Ramey, 2016). Hence, we want a model that is able to speak about the responses to these aggregate shocks
- Given the relevance in the academic literature and in policy circles, the **Smets and Wouters (2007) model** seems a sensible choice

Smets and Wotuers Model – Main Ingredients I

- Representative household with **habit formation** and preference for **leisure**

$$c_t = c_1 c_{t-1} + (1 - c_1) \mathbb{E}_t[c_{t+1}] + c_2 (l_t - \mathbb{E}_t[l_{t+1}]) - c_3 (r_t - \mathbb{E}_t[\pi_{t+1}] - \varepsilon_t^b)$$

- Households **invest in capital** given the **capital adjustment cost** they face

$$i_t = i_1 i_{t-1} + (1 - i_1) \mathbb{E}[i_{t+1}] + i_2 q_t + \varepsilon_t^i$$

where

$$q_t = q_1 \mathbb{E}[q_{t+1}] + (1 - q_1) \mathbb{E}r_{t+1}^k - (r_t - \mathbb{E}_t[\pi_{t+1}] - \varepsilon_t^b) \quad : \text{value of capital}$$

$$k_t = k_1 k_{t-1} + (1 - k_1) i_t + k_2 \varepsilon_t^i \quad : \text{installed capital LoM}$$

- **Aggregate production** uses installed capital ($k_t^S = k_{t-1} + z_t$) and labor services

$$y_t = \phi_p (\alpha k_t^S + (1 - \alpha) l_t + \varepsilon_t^a)$$

Smets and Wotuers Model – Main Ingredients II

- **Price stickiness** as in Calvo (1983) and **partial indexation** to lagged inflation gives rise to New-Keynesian Phillips curve

$$\pi_t = \pi_1 \pi_{t-1} + \pi_2 \mathbb{E}[\pi_{t+1}] - \pi_3 \mu_t^p + \varepsilon_t^p$$

- **Nominal wage stickiness** and partial indexation of wages to inflation

$$w_t = w_1 w_{t-1} + (1 - w_1) \mathbb{E}[w_{t+1} + \pi_{t+1}] - w_2 \pi_t + w_3 \pi_{t-1} - w_4 \mu_t^w + \varepsilon_t^w$$

- **Government spending** is exogenous and correlated with technology

$$\varepsilon_t^g = \rho_g \varepsilon_{t-1}^g + \eta_t^g + \rho_{ga} \eta_t^a$$

- The central bank sets the short-term interest rate according to the **monetary policy rule**

$$r_t = \rho_r r_{t-1} + (1 - \rho_r) (r_\pi \pi_t + r_y (y_t - y_t^p)) + r_{\Delta y} [(y_t - y_t^p) - (y_{t-1} - y_{t-1}^p)] + \varepsilon_t^r$$

MOMENT GENERATING FUNCTIONS

Local Projections (LP - IRFs)

- Some notation:

- * Let $\tilde{y}_t \in \{y_t, c_t, i_t, hw_t\}$ denote one of response variables of interest.
- * Let $\tilde{x}_t \in \{\eta_t^a, \eta_t^g, \eta_t^m\}$ denote the innovation of one of the three aggregate shocks.
- * Define the vector of contemporaneous r_t and lagged controls $w_t = \{\tilde{x}_t, \tilde{y}_t\}$

- Then, consider for each horizon $h = 0, 1, 2, \dots, H$ the *linear projections*:

$$\tilde{y}_{t+h} = \mu_h + \beta_h \tilde{x}_t + \gamma_h' r_t + \sum_{\ell=1}^p \delta_{h,\ell}' w_{t-\ell} + \zeta_{h,t} \quad (8)$$

where $\zeta_{h,t}$ is the projection residual and $\mu_h, \beta_h, \gamma_h, \{\delta_{h,\ell}'\}_{\ell=1}^p$ are the projection coefficients.

- **Definition.** The LP - IRFs of \tilde{y}_t with respect to \tilde{x}_t is given by $\{\beta_h\}_{h \geq 0}$ in the equation above.

Structural Vector Autoregression (SVAR - IRFs)

- Consider the multivariate linear VAR(p) projection:

$$w_t = c + \sum_{\ell=1}^p A_{\ell} w_{t-\ell} + u_t \quad (9)$$

where u_t is the projection residual and $c, \{A_{\ell}\}_{\ell=1}^p$ are the projection coefficients.

- Let $\Sigma_u \equiv \mathbb{E}[u_t u_t']$ and define the Cholesky decomposition $\Sigma_u = BB'$ where B is lower triangular with positive diagonal entries.
- Consider the corresponding recursive SVAR representation:

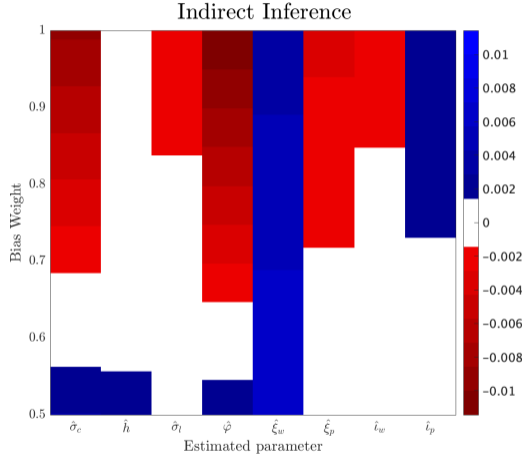
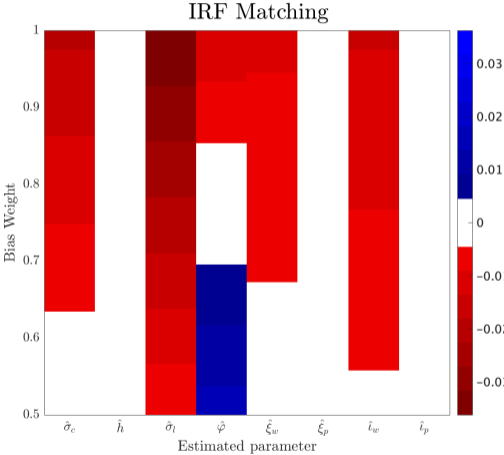
$$A(L)w_t = c + B\eta \quad (10)$$

where $A(L) = I - \sum_{\ell=1}^p A_{\ell} L^{\ell}$ and $\eta = B^{-1}u_t$. Define the lag polynomial $\sum_{\ell=0}^p C_{\ell} L^{\ell} = C(L) = A(L)^{-1}$.

- **Definition.** The SVAR - IRFs of \tilde{y}_t with respect to \tilde{x}_t is given by $\{\theta_h\}_{h \geq 0}$ with $\theta_h \equiv C_{2, \bullet, h} B_{\bullet, 1}$ where $\{C_{\ell}\}$ and B are defined above.

MONTE-CARLO RESULTS (OBSERVED SHOCK)

Parameter by parameter performance



$$z = \left(\mathcal{L}_\omega(\hat{\Theta}_i^{LP}, \Theta_i^*) - \mathcal{L}_\omega(\hat{\Theta}_i^{SVAR}, \Theta_i^*) \right) / \Theta_i^*$$

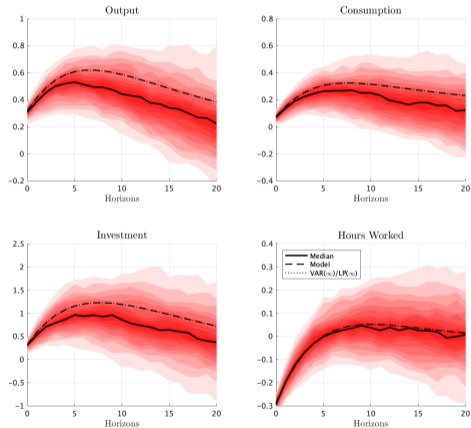
The role of the weighting matrix

| | IRF matching | | | | Indirect Inference | | | |
|-------------------------|--------------------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| | Identity Matrix | | | | | | | |
| <i>Local Projection</i> | 35.10 | 0.27 | 3.49 min | 18.70 | 32.54 | 0.39 | 42.88 min | 17.91 |
| <i>Structural VAR</i> | 35.23 | 0.41 | 3.93 min | 17.93 | 33.87 | 0.33 | 14.47 min | 18.39 |
| | Diagonal Matrix | | | | | | | |
| <i>Local Projection</i> | 34.44 | 0.22 | 3.61 min | 18.87 | 32.82 | 0.35 | 40.56 min | 18.22 |
| <i>Structural VAR</i> | 34.87 | 0.27 | 3.85 min | 18.20 | 34.17 | 0.31 | 11.55 min | 18.62 |
| | Optimal Weighting Matrix | | | | | | | |
| <i>Local Projection</i> | 33.63 | 0.04 | 3.07 min | 21.56 | 32.69 | 0.06 | 35.56 min | 21.41 |
| <i>Structural VAR</i> | 34.17 | 0.05 | 3.20 min | 20.80 | 34.26 | 0.08 | 10.69 min | 20.90 |

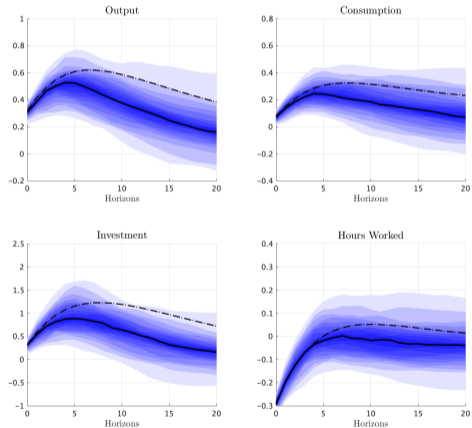
MONTE-CARLO RESULTS (RECURSIVE IDENTIFICATION)

TFP Shock: recursive assumption is correct in Sm & Wo (2007)

Local Projection



SVAR

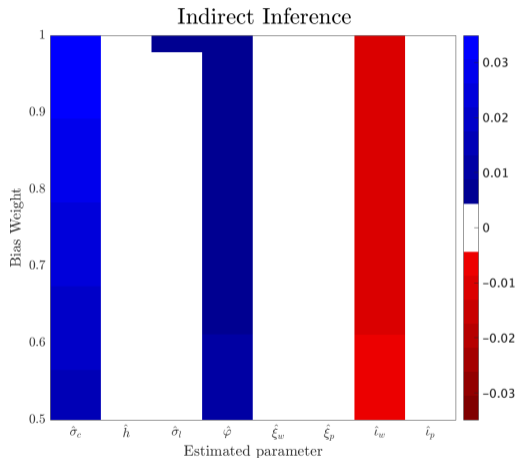
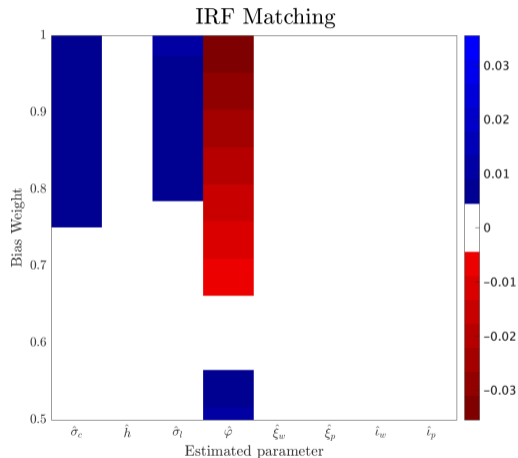


TFP Shock: if assumptions are right, identification does not matter

- If *recursive assumptions are correct*, the identification strategy does not play a role in the estimation
- **Main lesson still holds:** use LPs for *IRF matching* exercises and VARs for *Ind. Inf.*
- **Model fit:** J_{unt}^* is large \implies not great idea to target just TFP shocks in the Smets-Wouters model

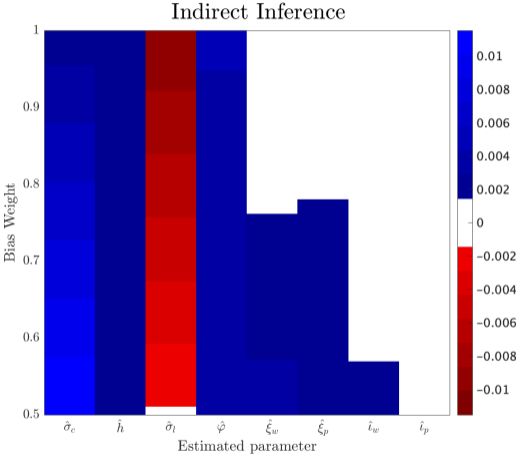
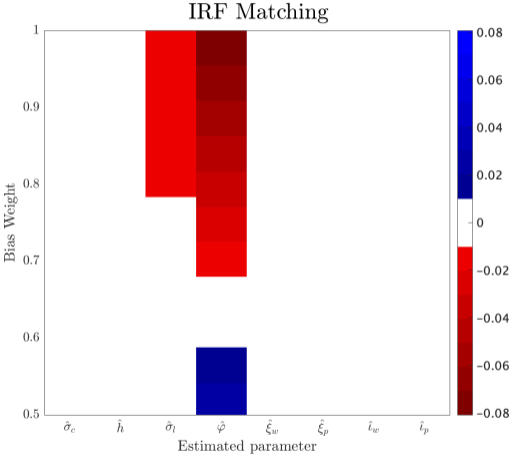
| | IRF matching | | | | Indirect Inference | | | |
|-------------------------|--------------|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| <i>Local Projection</i> | 1.05 | 0.67 | 2.87 min | 37.30 | 0.70 | 0.84 | 42.41 min | 35.92 |
| <i>Structural VAR</i> | 2.53 | 1.07 | 3.11 min | 35.74 | 0.97 | 0.66 | 14.34 min | 37.31 |

TFP Shock: it is all about the investment adjustment cost $\hat{\varphi}$



$$z = \left(\mathcal{L}_\omega(\hat{\Theta}_i^{LP}, \Theta_i^*) - \mathcal{L}_\omega(\hat{\Theta}_i^{SVAR}, \Theta_i^*) \right) / \Theta_i^*$$

Monetary Policy: parameter by parameter performance



$$z = \left(\mathcal{L}_\omega(\hat{\Theta}_i^{LP}, \Theta_i^*) - \mathcal{L}_\omega(\hat{\Theta}_i^{SVAR}, \Theta_i^*) \right) / \Theta_i^*$$

MONTE-CARLO RESULTS (MEASUREMENT ERROR)

Proxy shocks: bad news for the structural estimates

- The **estimation outcome is significantly worse** for both LPs and VARs as well as for the *IRF matching* and *Ind. Inf.* estimators relative to the observed shock case.
- These findings also apply to other sources of variation such as monetary or fiscal policy shocks.
- Does it get worse when the proxy is correlated with other shocks? Does unit normalization of the IRFs help in identifying responses?

| | IRF matching | | | | Indirect Inference | | | |
|------------------|---|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| | <i>True technology shock (η_t^a)</i> | | | | | | | |
| Local Projection | 1.05 | 0.67 | 2.87 min | 37.30 | 0.70 | 0.84 | 42.41 min | 35.92 |
| Structural VAR | 2.53 | 1.07 | 3.11 min | 35.74 | 0.97 | 0.66 | 14.34 min | 37.31 |
| | <i>Proxied technology shock ($\eta_t^{a,obs} = \eta_t^a + \sigma_v v_t$)</i> | | | | | | | |
| Local Projection | 1.79 | 1.25 | 3.05 min | 34.30 | 1.35 | 1.40 | 40.23 min | 33.31 |
| Structural VAR | 3.41 | 1.70 | 2.80 min | 33.47 | 1.70 | 1.18 | 13.74 min | 34.39 |

Govn't spending and its correlation with technology

- The J^* is again much larger than in the observed shock case or in the proxy measure with classical measurement error, and for both estimation approaches.
 - * *Ind. Inf.* is not robust to this type of misspecification, unlike for (misspecified) recursive shocks
- The model fit, J_{unt}^* , improves in the *IRF matching* because the IRF with the shock (not just the innovation) captures some information about technology shocks.

| | IRF matching | | | | Indirect Inference | | | |
|-------------------------|--|-------|----------|-------------|--------------------|-------|-----------|-------------|
| | J_{irf} | J^* | Time | J_{unt}^* | J_{smm} | J^* | Time | J_{unt}^* |
| | <i>Government spending innovation (η_t^g)</i> | | | | | | | |
| <i>Local Projection</i> | 53.59 | 0.07 | 4.14 min | 9.43 | 48.45 | 0.02 | 44.82 min | 8.40 |
| <i>Structural VAR</i> | 49.09 | 0.05 | 4.32 min | 8.79 | 47.03 | 0.03 | 14.42 min | 8.42 |
| | <i>A correlated government spending proxy ($\varepsilon_t^{g,obs}$)</i> | | | | | | | |
| <i>Local Projection</i> | 30.82 | 0.34 | 4.09 min | 7.80 | 39.05 | 0.35 | 46.13 min | 10.15 |
| <i>Structural VAR</i> | 31.45 | 0.34 | 4.19 min | 7.78 | 42.42 | 0.40 | 14.20 min | 10.53 |