

Macroeconomic dynamics in the UK mortgage market

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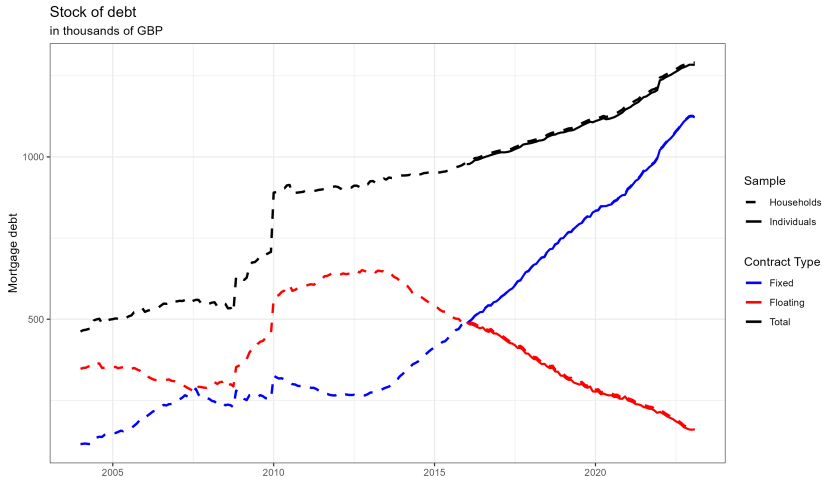
- Inflationary pressures call for **rises in the policy rate R_t**
 - * Bank of England have raised their interest rate to 5.25% from 0.1% since December 2021
 - * Other central banks have implemented similar measures
- Higher rates affect demand (consumption) and financial stability primarily through the **housing market**
- Importantly, rising mortgage costs affect the economy differently depending on what type of **mortgage contracts** households have
- Typically, there are two types of contracts
 - * Fixed rate mortgages \rightarrow high R_t matters for new mortgages and when refinancing
 - * Adjustable rate mortgages \rightarrow almost 1 to 1 pass through between R_t and mortgage rate
- But the **UK (mortgage market) is different . . .**

- Empirically:
 - * Use Product Sales Data (PSD) on mortgage originations in the UK
 - * Describe the distribution of mortgage contracts in the UK (interest rate, duration, etc.)
- Theoretically:
 - * Modify Greenwald (2018) macro-housing model to reflect some UK mortgage market features
 - * Study the macroeconomic transmission of various shocks under different mortgage contract types: FRM, ARM, Hybrid Rate Mortgage (HRM)
 - * Study the effects of the recent increases in the policy rate on real outcomes when mortgage contracts are similar to those hold by UK households

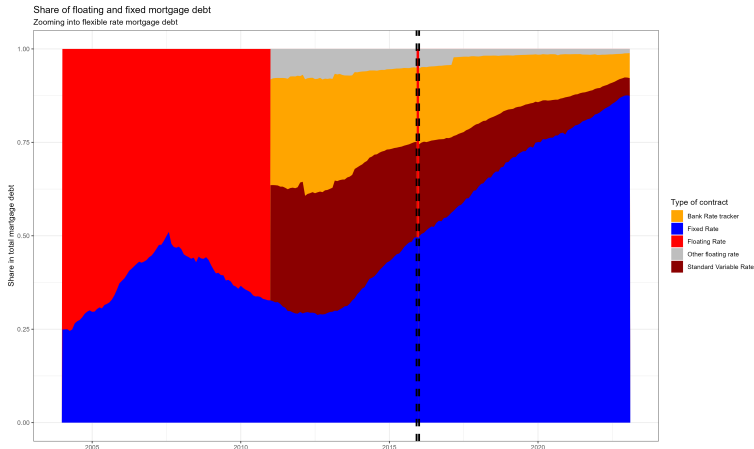
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THE UK MORTGAGE MARKET

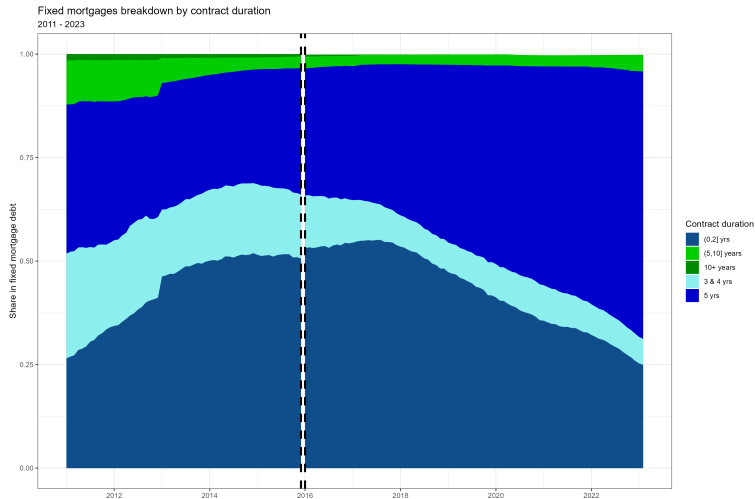
The stock of mortgage debt continues to grow



- The share of fixed mortgage debt has steadily increased from 35% of total debt in 2014 to more than 75% in 2023
- The remaining 25% is split between Standard Variable Rate and BoE Bank Rate Tracker

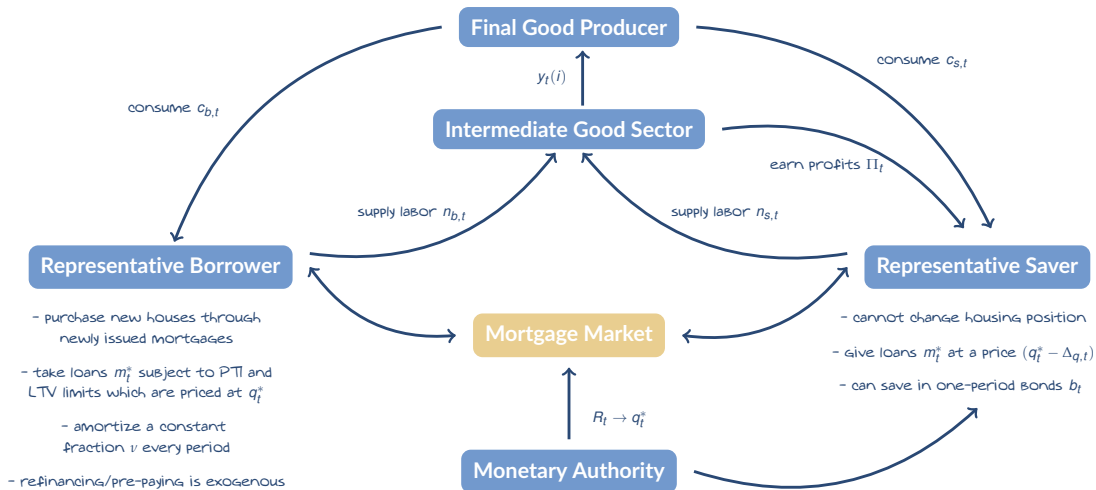


Fixed rate contracts have a short duration



- 2-year and 5-year contracts are the most popular contracts in the UK
- Note that these contracts revert to a floating rate after the fixation period

THE MODEL ECONOMY



- Chooses *consumption* $c_{b,t}$, *labor* supply $n_{b,t}$, the size of newly purchased houses $h_{b,t}^*$, and the face value of newly issued *mortgages* m_t^*
- to maximize lifetime expected discounted utility using the aggregate utility function

$$u(c_{b,t}, h_{b,t-1}, n_{b,t}) = \log(c_{b,t}/\chi_b) + \zeta \log(h_{b,t-1}/\chi_b) - \eta_b \frac{(n_{b,t}/\chi_b)^{1+\varphi}}{1+\varphi} \quad (1)$$

- subject to the **budget constraint**

$$c_{b,t} \leq (1 - \tau_y) w_t n_{b,t} - \pi_t^{-1} ((1 - \tau_y) x_{b,t-1} + v m_{t-1}) + \rho_b (m_t^* - (1 - v) \pi_t^{-1} m_{t-1}) - \delta p_t^h h_{b,t-1} - \rho_b p_t^h (h_{b,t}^* - h_{b,t-1}) + T_{b,t} \quad (2)$$

- the **debt constraint**

$$m_t^* \leq \bar{m}_t = \underbrace{\left((\theta^{PTI} - \omega) w_t n_{t,i} e_{t,i} \right) / (q_t^* + \alpha)}_{=\bar{m}_t^{PTI}} \int^{\bar{e}_t} e_i d\Gamma_e(e_i) + \underbrace{\theta^{LTV} p_t^h h_{i,t}^*}_{=\bar{m}_t^{LTV}} (1 - \Gamma_e(\bar{e}_t)) \quad (3)$$

- and **laws of motion** for total start-of-period debt balances m_{t-1} , total promised payments on existing debt $x_{t-1} \equiv q_{t-1} m_{t-1}$ and total start-of-period borrower housing $h_{b,t-1}$

- Two benchmarks:

- * *Fixed rate mortgage contract (FRM)*

$$m_t = \rho_b m_t^* + (1 - \rho_b)(1 - \nu)\pi_t^{-1} m_{t-1}$$
$$x_{b,t}^{FRM} = \rho_b q_t^* m_t^* + (1 - \rho_b)(1 - \nu)\pi_t^{-1} x_{b,t-1}$$

- * *Flexible rate mortgage contract (ARM)*

$$m_t = \rho_b m_t^* + (1 - \rho_b)(1 - \nu)\pi_t^{-1} m_{t-1}$$
$$x_{b,t}^{ARM} = q_t^* m_t$$

- **UK Mortgage Framework** (e.g. 2 periods fixed, then adjustable contract)

$$m_t = \rho_b m_t^* + (1 - \rho_b)(1 - \nu)\pi_t^{-1} m_{t-1}$$
$$x_{b,t}^{HRM} = \rho_b q_t^* m_t^* + (1 - \rho_b)(1 - \nu)\pi_t^{-1} \rho_b q_{t-1}^* m_{t-1}^* + (1 - \rho_b)^2 (1 - \nu)^2 \pi_t^{-1} \pi_{t-1}^{-1} q_{t-1}^* m_{t-1}$$

- Chooses *consumption* $c_{s,t}$, *labor* supply $n_{s,t}$, one period bonds b_t , and the face value of newly issued mortgages m_t^*

- to maximize lifetime expected discounted utility using the aggregate utility function

$$u(c_{s,t}, n_{s,t}) = \log(c_{s,t}/\chi_s) + \zeta \log(\tilde{H}_{s,t-1}/\chi_s) - \eta_s \frac{(n_{s,t}/\chi_s)^{1+\varphi}}{1+\varphi} \quad (4)$$

- subject to the **budget constraint**

$$c_{s,t} \leq (1 - \tau_y) w_t n_{s,t} + \pi_t^{-1} x_{s,t-1} - \rho_b \left(m_t^* - (1 - \nu) \pi_t^{-1} m_{t-1} \right) - \delta p_t^h \tilde{H}_s - \left(R_t^{-1} b_t - \pi_t^{-1} b_{t-1} \right) + \Pi_t + T_{s,t} \quad (5)$$

- and **laws of motion** for total start-of-period debt balances m_{t-1} , and total promised payments on existing debts:

$$x_{s,t}^{FRM} = \rho_b (q_t^* - \Delta_{q,t}) m_t^* + (1 - \rho_b)(1 - \nu) \pi_t^{-1} x_{s,t-1} \quad \text{or} \quad x_{s,t}^{ARM} = (q_t^* - \Delta_{q,t}) m_t \quad (6)$$

where $\Delta_{q,t}$ is a proportional tax on all future mortgage payments that follows a stochastic process (term premium shock = innovation on the process)

- Production

- * A competitive final good producer: $\max_{y_t(i)} P_t \left[\int_0^1 y_t(i)^{\frac{\lambda-1}{\lambda}} di \right]^{\frac{\lambda}{\lambda-1}} - \int_0^1 P_t(i) y_t(i) di$
- * A continuum of intermediate good producers that choose price $P_t(i)$ and operates a linear technology $y_t(i) = a_t n_t(i)$ to meet the final's good producer demand.
- * Intermediate good producers are subject to *price stickiness* – Calvo pricing with indexation.

- Monetary authority: it follows a Taylor rule of the form

$$\begin{aligned} \log R_t = & \log \bar{\pi}_t + \phi_r (\log R_{t-1} - \log \bar{\pi}_{t-1}) \\ & + (1 - \phi_r) [(\log R_{ss} - \log \pi_{ss}) + \psi_\pi (\log \pi_t - \log \bar{\pi}_t)] \end{aligned} \quad (7)$$

where $\bar{\pi}_t$ is a time-varying inflation target

EQUILIBRIUM CONDITIONS

- The optimality of new debt, m_t^* , determines the mortgage coupon rate, q_t^* .
- **Borrower optimality:**

$$1 = \Omega_{b,t}^m + \Omega_{b,t}^x q_t^* + \mu_t \quad (8)$$

where μ_t is the multiplier on the aggregate credit limit, and $\Omega_{b,t}^m$ and $\Omega_{b,t}^x$ are the marginal continuation costs to the borrower of taking an additional dollar of face value debt and of promising an additional dollar of initial payments

- **Saver optimality:**

$$1 = \Omega_{s,t}^m + \Omega_{s,t}^x (q_t^* - \Delta_{q,t}) \quad (9)$$

where $\Omega_{s,t}^m$ and $\Omega_{s,t}^x$ are the marginal continuation benefits of an additional unit of face value debt and an additional dollar of promised initial payments

- **Borrower (saver) marginal continuation costs (benefits) differ depending on the contract type:**
(a) FRM, (b) ARM, (c) HRM

- Fixed Rate Mortgage Contracts

$$\Omega_{b,t}^m = \mathbb{E}_t \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \left(\nu + (1 - \nu) \rho_{t+1} + (1 - \nu)(1 - \rho_{t+1}) \Omega_{b,t+1}^m \right) \right] \quad (10)$$

$$\Omega_{b,t}^x = \mathbb{E}_t \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \left((1 - \tau_y) + (1 - \nu)(1 - \rho_{t+1}) \Omega_{b,t+1}^x \right) \right] \quad (11)$$

- Adjustable Rate Mortgage Contracts

$$\Omega_{b,t} = \mathbb{E}_t \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \left((1 - \tau_y) q_t^* + \nu + (1 - \nu) \rho_{t+1} + (1 - \nu)(1 - \rho_{t+1}) \Omega_{b,t+1} \right) \right] \quad (12)$$

$$\Omega_{b,t}^x = 0 \quad (13)$$

- Hybrid Rate Mortgage Contracts

$$\Omega_{b,t}^m = \mathbb{E}_t \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \left(\nu + (1 - \nu) \rho_{t+1} + (1 - \nu)(1 - \rho_{t+1}) \Omega_{b,t+1}^m \right) \right] \quad (14)$$

$$\Omega_{b,t}^x = \mathbb{E}_t \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} (1 - \tau_y) \right] + \sum_{\tau=1}^{T-1} \mathbb{E}_{t+\tau} \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \left(\prod_{j=1}^{\tau} \Lambda_{t+1+j,t+j}^b \pi_{t+1+j}^{-1} (1 - \rho_{t+j}) \right) (1 - \tau_y) \right] \quad (15)$$

INTEREST RATE TRANSMISSION

- **Constraint Switching Effect**

▷ Go to IRFs

- * The interaction of LTV and PTI constraints creates a transmission chain from interest rates into house prices and amplifies the debt response
 - A reduction in rates directly loosens the PTI constraint which in turn increases the share of LTV-constrained borrowers
 - These borrowers can increase their borrowing limit with additional collateral which boosts housing demand, rising the price-to-rent ratio
 - Higher house price increase collateral values, relaxing LTV constraints, and leading to a larger response of debt

- **Frontloading Effect**

▷ Go to IRFs

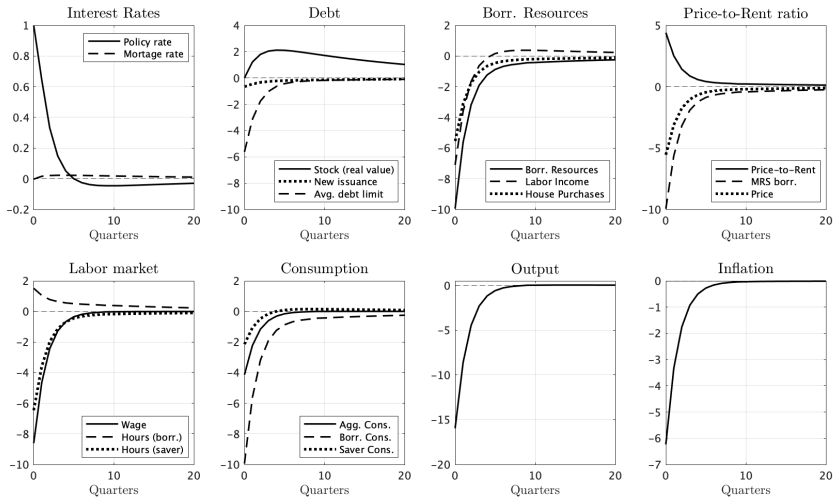
- * Looser credit conditions (e.g. lower mortgage rates) lead to a large increase in borrower consumption as they refinance more quickly
- * As a result, output rises in the short run before intermediate firms reset their prices

- **Transitory shocks** ▷ Go to IRFs
 - * *Term premium shock* imposes a temporary shift in mortgage rates
 - * **Under FRM** borrowers refinance and take larger loans to secure cheaper credit, leading to
 - a 2.5 larger mortgage debt increase after 2 years, ...
 - a 35% larger price to rent ratio upon impact, and
 - a 6% bigger output response on impact than under ARM
 - * *Redistribution* from savers to borrowers is **larger under FRM**
 - * *Endogenous refinancing* amplifies household consumption, output and inflation responses only under FRM
 - For a constant refinancing rate $\rho = 0.145$, output and inflation responses are similar under both contracts
- **Permanent shocks** ▷ Go to IRFs
 - * *Inflation target shock* imposes a near permanent change in mortgage rates
 - * *Aggregate variable responses* are **similar** across contract types
 - * *Redistribution* from savers to borrowers **larger under ARM** (except from $t = 0$)

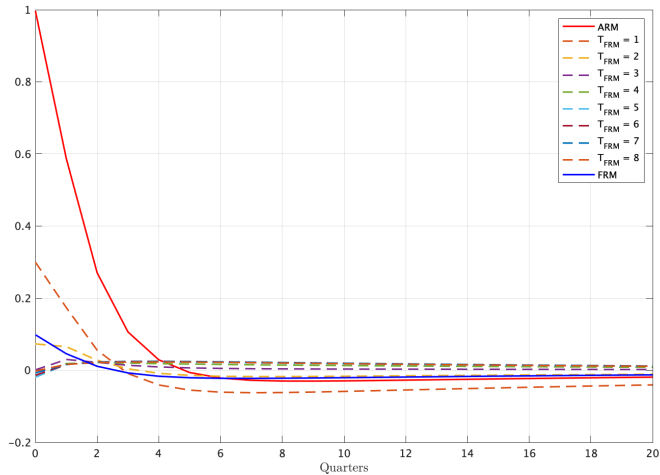
- Recall that typical contract in UK mortgage market features fixed mortgage rates for a short (2-5 year) duration after reverting to a variable rate
- A first pass would be to study an economy with **high refinancing rates** and **fixed rate mortgages**. Two approaches:
 - * Reduce refinancing costs while keeping endogenous choice
 - Leads to a larger pre-payment rates, more debt and higher prices-to-rent ratio [▷ Go to figure](#)
 - But it is inconsistent with the UK framework as fees are prohibitive during the fixation period
 - * Making the *refinancing* decision *exogenous*
 - Exogenous prepayment downplays the differential response of consumption, output and inflation to *transitory shocks* in the FRM vs. ARM economies [▷ Go to IRFs](#)
 - The responses to *permanent shocks* in the FRM vs. ARM economies are similar despite the higher refinancing rates [▷ Go to IRFs](#)
 - Berger et al. (2021) show that refinancing rates are fairly constant when rates gap are negative. This is typically the case in hike cycles. Supportive evidence for exogenous pre-payment

- **Conventional monetary policy** (policy rate movements) affects mortgage rates differently depending on the mortgage contract (FRM vs ARM) and refinancing rate [▷ Go to figure](#)
 - * One-to-one pass-through for ARM, independently of the refinancing rate
 - * Pass-through is increasing in the refinancing rate for FRM, but always below one-to-one
- For a **FRM economy** with a refinancing rate of $\rho_b = 0.145$, a 1% increase in the policy rate leads to
 - * an immediate **fall in the inflation rate** because the economy slows down as households cut on consumption, with **borrower's consumption falling by more** than that of savers
 - * deflation leads to an **increase in the real value of debt** despite a decrease in loan's size associated with higher mortgage rates
 - * **more expensive credit reduces housing demand** and house price falls, however, the price to rent ratio rises
- For a **ARM economy**, the same 1% increase in the policy rate results in similar quantitative and qualitative responses despite the **larger increase in mortgage payments**
 - * Implication: New Keynesian channel dominates (see Garriga et al., 2021)

Hybrid Rate Mortgages (2yr HRM)



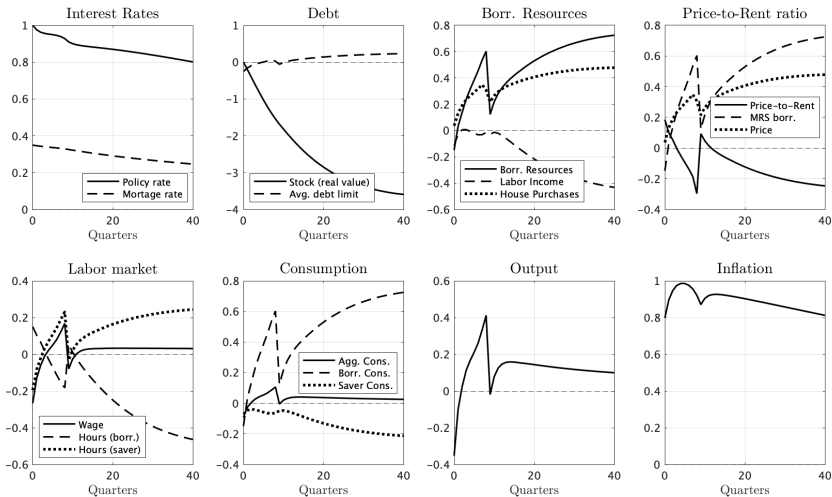
Pass-Through in HRM with different durations



▷ FRM IRFs

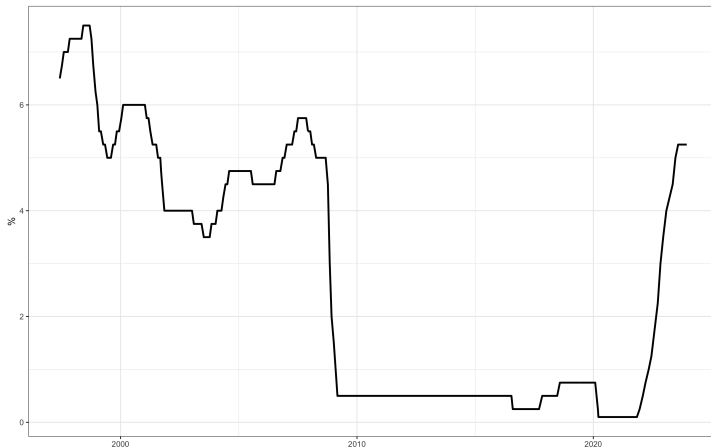
▷ ARM IRFs

Hybrid Rate Mortgages (2yr HRM)

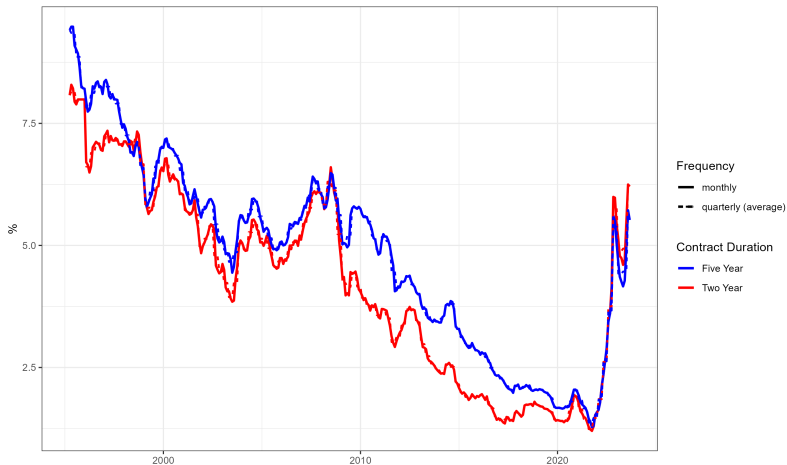


APPENDIX

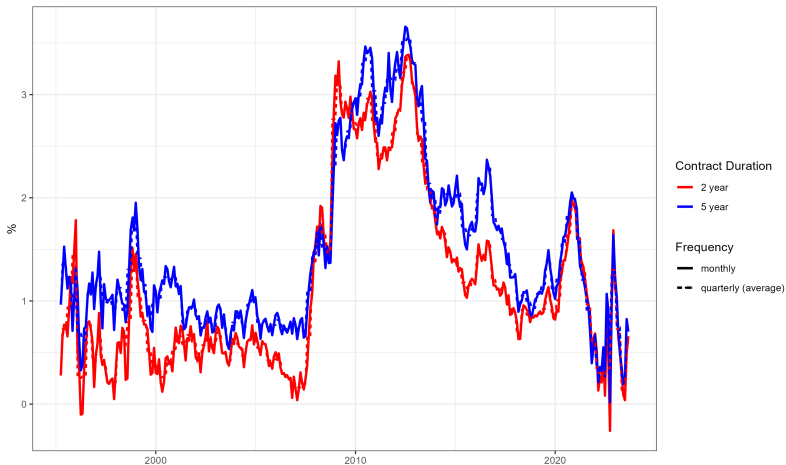
Bank Rate
1997-2023



Rates on 75% LTV Mortgages
1995 - 2023



Mortgage Spreads
1995 - 2023



- Typical UK mortgage contracts are hybrid between ARM and FRM. They are T periods under fixed rates before switching to an adjustable one
- Hybrid Rate Mortgages can be generalized to embrace these two contracts
 - * ARM \equiv HRM with $T = 0$
 - * FRM \equiv HRM with $T = \infty$
- In general, for a T -period adjustable mortgage, the law of motion of promised payments is:

$$x_{b,t}^{HRM} = \rho_b q_t^* m_t^* + \left[\sum_{\tau=1}^{T-1} \left(\prod_{i=0}^{\tau-1} (1 - \rho_b)(1 - v) \pi_{t-i}^{-1} \right) \rho_b q_{t-\tau}^* m_{t-\tau}^* \right] + \left(\prod_{i=0}^{T-1} (1 - \rho_b)(1 - v) \pi_{t-i}^{-1} \right) q_{t-T}^* m_{t-T}^*$$

- Fixed Rate Mortgage Contracts

$$\Omega_{s,t}^m = \mathbb{E}_t \left[\Lambda_{t,t+1}^s \pi_{t+1}^{-1} (\rho_b (1 - \nu) + (1 - \rho_b)(1 - \nu) \Omega_{s,t+1}^m) \right] \quad (16)$$

$$\Omega_{s,t}^x = \mathbb{E}_t \left[\Lambda_{t,t+1}^s \pi_{t+1}^{-1} (1 + (1 - \rho_b)(1 - \nu) \Omega_{s,t+1}^x) \right] \quad (17)$$

- Adjustable Rate Mortgage Contracts

$$\Omega_{s,t} = \mathbb{E}_t \left[\Lambda_{t,t+1}^s \pi_{t+1}^{-1} ((q_t^* - \Delta_{q,t}) + (1 - \nu) \rho_b + (1 - \nu)(1 - \rho_b) \Omega_{s,t+1}) \right] \quad (18)$$

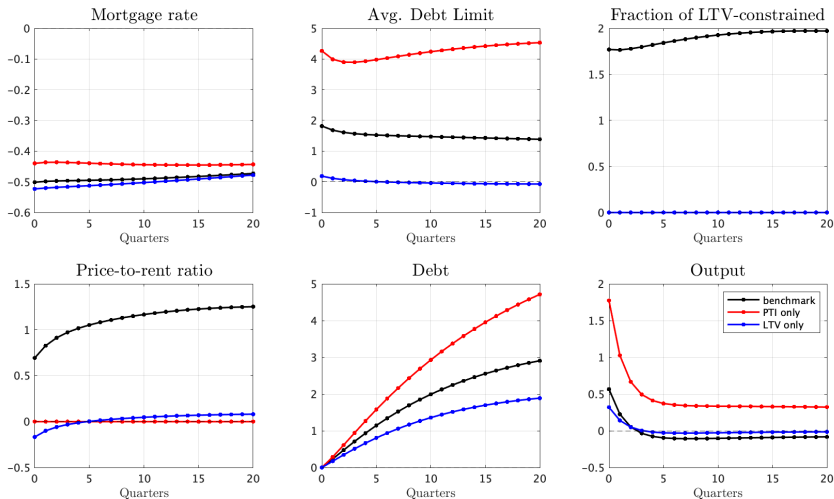
$$\Omega_{b,t}^x = 0 \quad (19)$$

- Fixed Period Adjustable Mortgage Contracts

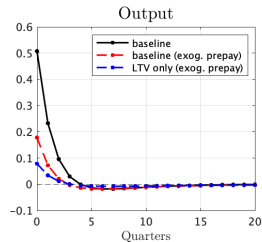
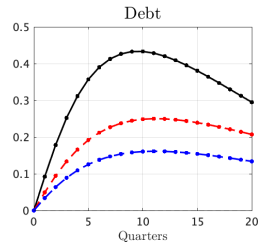
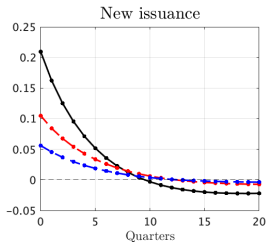
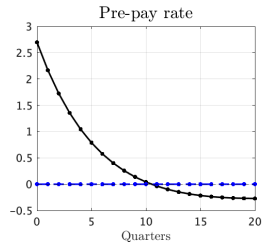
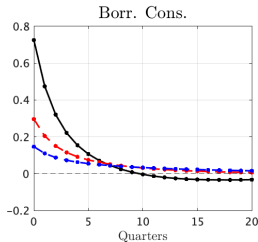
$$\Omega_{s,t}^m = \mathbb{E}_t \left[\Lambda_{t,t+1}^s \pi_{t+1}^{-1} (\rho_b (1 - \nu) + (1 - \rho_b)(1 - \nu) \Omega_{s,t+1}^m) \right] \quad (20)$$

$$\Omega_{b,t}^x = \mathbb{E}_t \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \right] + \sum_{\tau=1}^{T-1} \mathbb{E}_{t+\tau} \left[\Lambda_{t,t+1}^b \pi_{t+1}^{-1} \left(\prod_{j=1}^{\tau} \Lambda_{t+1+j,t+j}^b \pi_{t+1+j}^{-1} (1 - \rho_b)(1 - \nu) \right) \right] \quad (21)$$

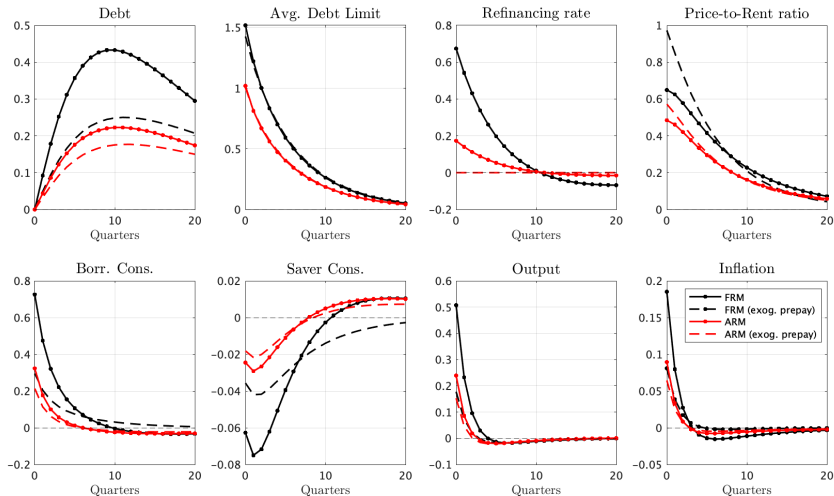
Constraint Switching Effect – Inflation Target Shock



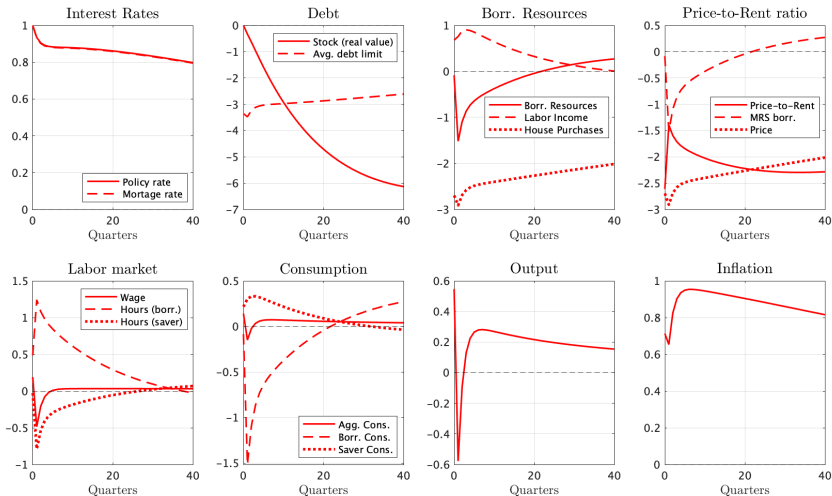
Frontloading Effect – Term Premium Shock

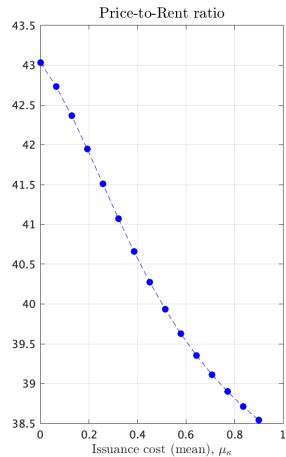
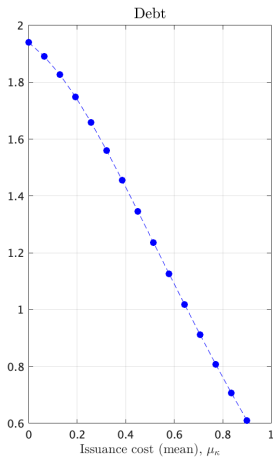
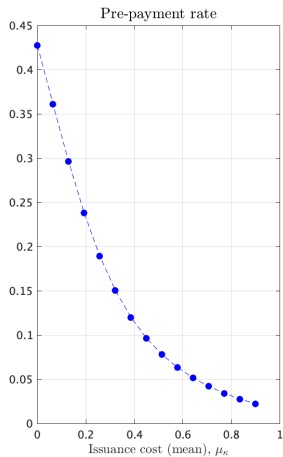


Transitory Shock – FRM vs ARM

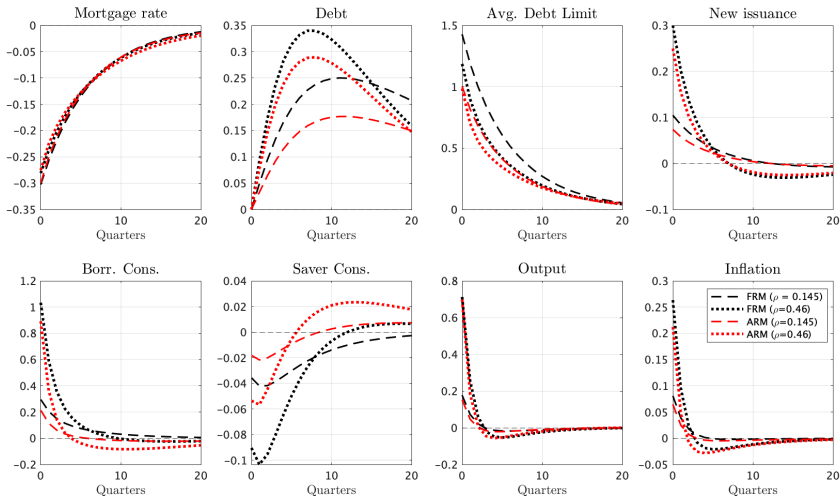


Permanent Shock – FRM vs ARM

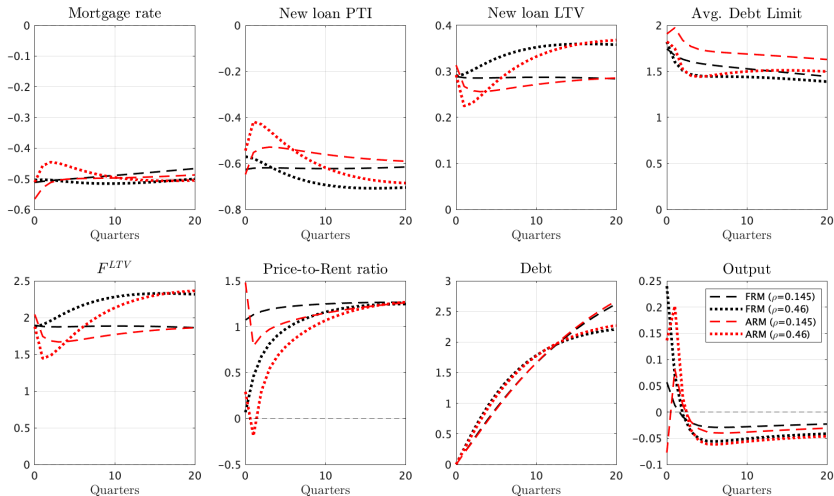




High vs. Low Refinancing Rate – Temporary Shock



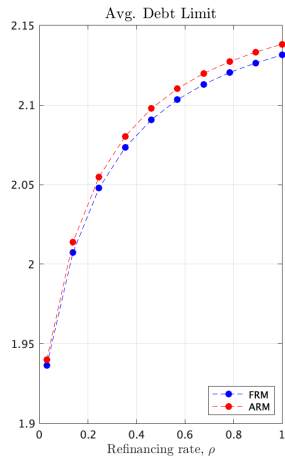
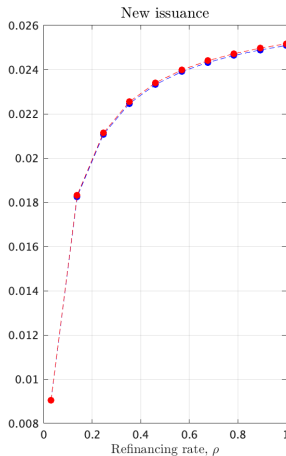
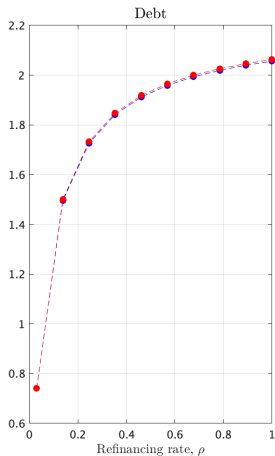
High vs. Low Refinancing Rate – Permanent Shock



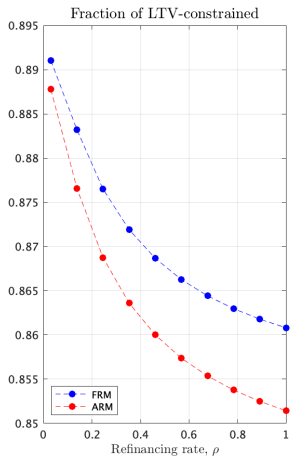
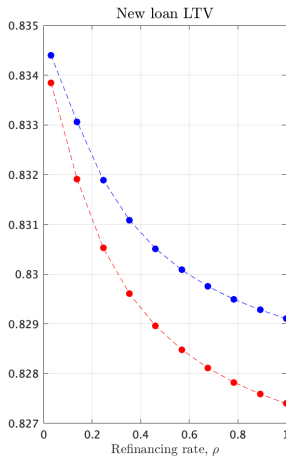
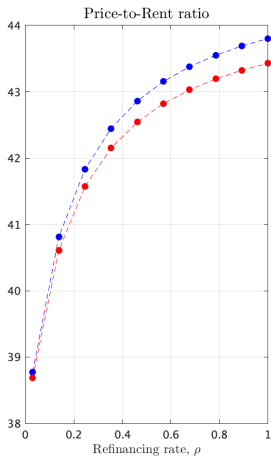
- An **increase** in the exogenous refinancing rate ρ_b leads to:
 - * Higher levels of mortgage debt via new issuance and bigger loans [▷ Go to figure](#)
 - * More housing demand, which puts upward pressure in the house price to rent ratio and loosens the LTV limit [▷ Go to figure](#)
 - * A redistribution of resources from borrowers to savers despite not affecting the equilibrium mortgage coupon [▷ Go to figure](#)

[▷ Back](#)

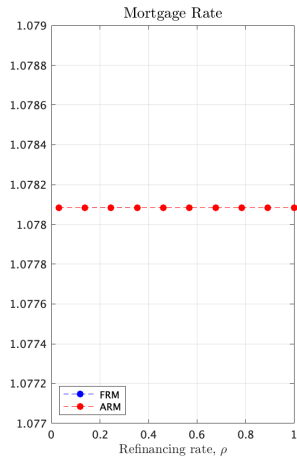
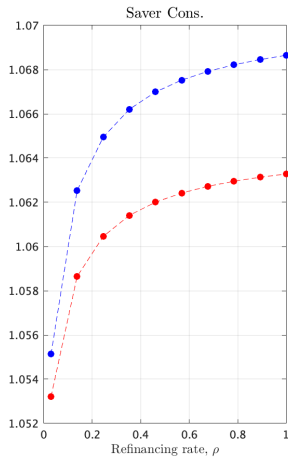
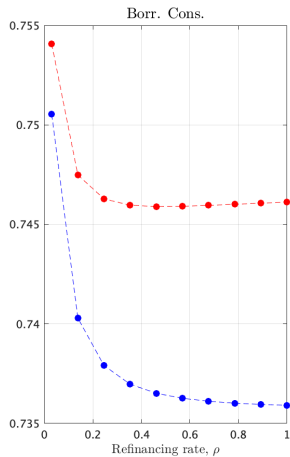
More refinancing leads to more debt



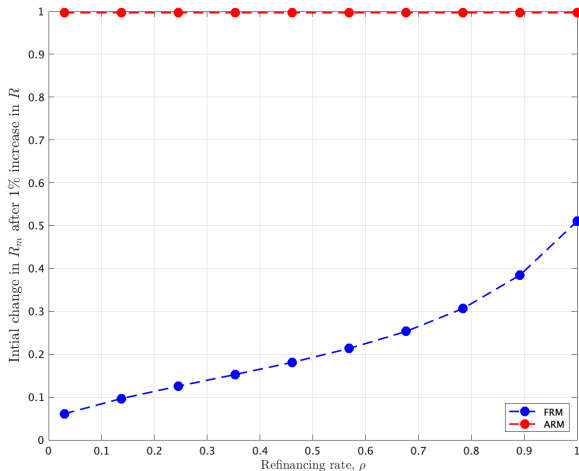
More refinancing boosts housing demand



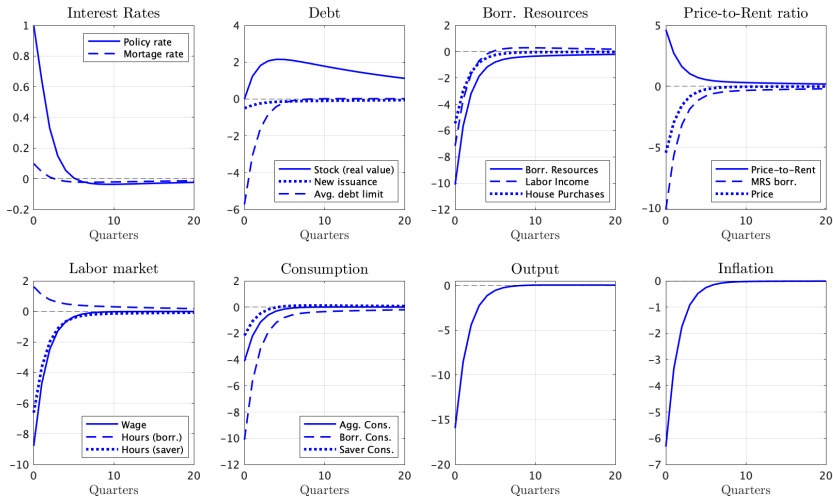
More refinancing redistributes from borr. to savers



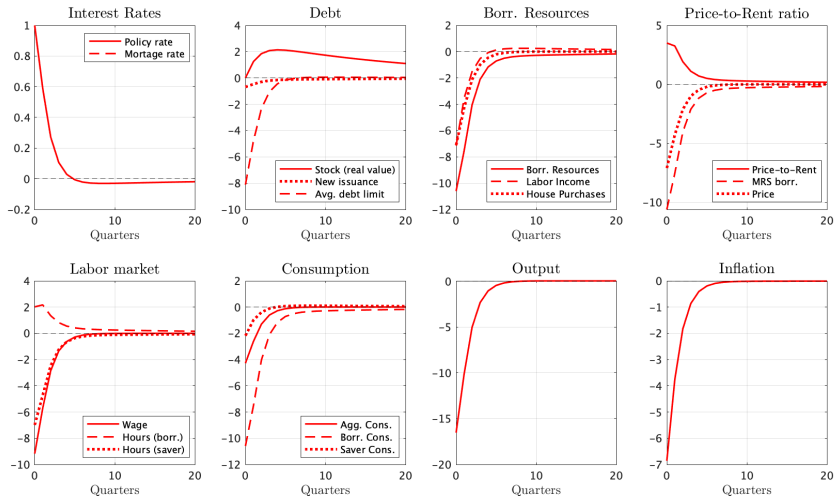
Monetary Policy Pass-Through to Mortgage Rates



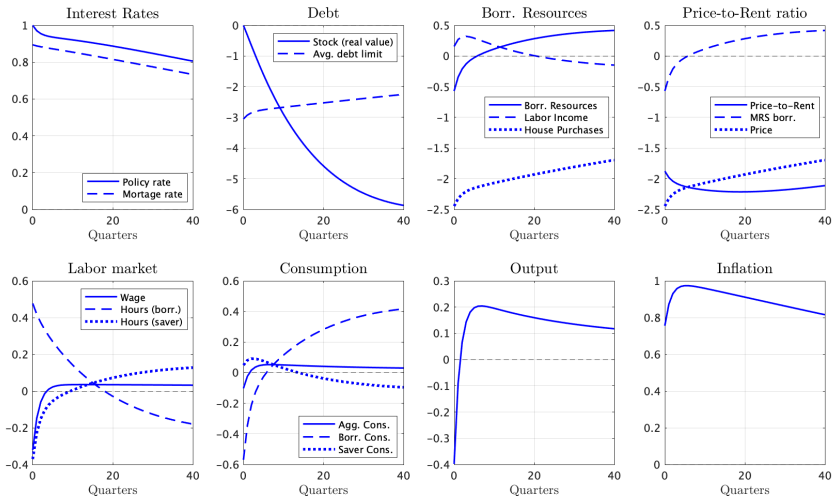
Temporary Monetary Shock in FRM economy



Temporary Monetary Shock in FRM economy



Inflation Target Shock in FRM economy



Inflation Target Shock in FRM economy

